



**University of
Zurich**^{UZH}

**Zurich Open Repository and
Archive**

University of Zurich
University Library
Strickhofstrasse 39
CH-8057 Zurich
www.zora.uzh.ch

Year: 2018

Sequential superconductor–Bose insulator–Fermi insulator phase transitions in quasi-two-dimensional -WSi

Zhang, Xiaofu ; Schilling, Andreas

Abstract: A zero-temperature magnetic-field-driven superconductor to insulator transition (SIT) in quasi-two-dimensional superconductors is expected to occur when the applied magnetic field crosses a certain critical value [S. L. Sondhi, S. M. Girvin, J. P. Carini, and D. Shahar, *Rev. Mod. Phys.* 69, 315 (1997); A. M. Goldman, *Int. J. Mod. Phys. B* 24, 4081 (2010)]. A fundamental question is whether this transition is due to the localization of Cooper pairs or due to the destruction of them. Here we address this question by studying the SIT in amorphous WSi. Transport measurements reveal the localization of Cooper pairs at a quantum critical field B_{1c} (Bose insulator), with a product of the correlation length and dynamical exponents $z \approx 4/3$ near the quantum critical point. Beyond B_{1c} , superconducting fluctuations still persist at finite temperatures. Above a second critical field $B_{2c} > B_{1c}$, the Cooper pairs are destroyed and the film becomes a Fermi insulator. The different phases all merge at a tricritical point at finite temperatures with $z = 2/3$. Our results suggest a sequential superconductor to Bose insulator to Fermi insulator phase transition, which differs from the conventional scenario involving a single quantum critical point.

DOI: <https://doi.org/10.1103/physrevb.97.214524>

Posted at the Zurich Open Repository and Archive, University of Zurich

ZORA URL: <https://doi.org/10.5167/uzh-159701>

Journal Article

Published Version

Originally published at:

Zhang, Xiaofu; Schilling, Andreas (2018). Sequential superconductor–Bose insulator–Fermi insulator phase transitions in quasi-two-dimensional -WSi. *Physical review. B*, 97(21):214524.

DOI: <https://doi.org/10.1103/physrevb.97.214524>

Sequential superconductor–Bose insulator–Fermi insulator phase transitions in quasi-two-dimensional α -WSi

Xiaofu Zhang and Andreas Schilling

Physik-Institut, Universität Zürich, Winterthurerstrasse 190, Zürich CH-8057, Switzerland



(Received 28 February 2018; revised manuscript received 14 June 2018; published 29 June 2018)

A zero-temperature magnetic-field-driven superconductor to insulator transition (SIT) in quasi-two-dimensional superconductors is expected to occur when the applied magnetic field crosses a certain critical value [S. L. Sondhi, S. M. Girvin, J. P. Carini, and D. Shahar, *Rev. Mod. Phys.* **69**, 315 (1997); A. M. Goldman, *Int. J. Mod. Phys. B* **24**, 4081 (2010)]. A fundamental question is whether this transition is due to the localization of Cooper pairs or due to the destruction of them. Here we address this question by studying the SIT in amorphous WSi. Transport measurements reveal the localization of Cooper pairs at a quantum critical field B_c^1 (Bose insulator), with a product of the correlation length and dynamical exponents $z\nu \sim 4/3$ near the quantum critical point. Beyond B_c^1 , superconducting fluctuations still persist at finite temperatures. Above a second critical field $B_c^2 > B_c^1$, the Cooper pairs are destroyed and the film becomes a Fermi insulator. The different phases all merge at a tricritical point at finite temperatures with $z\nu = 2/3$. Our results suggest a sequential superconductor to Bose insulator to Fermi insulator phase transition, which differs from the conventional scenario involving a single quantum critical point.

DOI: [10.1103/PhysRevB.97.214524](https://doi.org/10.1103/PhysRevB.97.214524)

Zero-temperature quantum phase transitions (QPTs) between different quantum states are expected to occur when a control parameter crosses over a certain critical value [1–3]. The zero-temperature superconductor to insulator QPT in two dimensions, for example, is a well-documented manifestation for such a QPT [2], which can be tuned by control parameters such as external magnetic field, electrical field, charge density, disorder, or thickness [2,4–7]. In the vicinity of the quantum critical point (QCP), a quantum critical region is formed due to quantum fluctuations, and the physical behaviors of QPTs can be perceived through measurements at nonzero temperature within the quantum critical region [2].

The superconducting state is characterized by an order parameter, in terms of amplitude (related to energy gap Δ or Cooper-pair density n_s) and phase ϕ . As a result, a superconductor to insulator transition (SIT) can be grouped into two distinct classes, with fermionic and with bosonic descriptions. The fermionic scenario describes the SIT as a result of the amplitude fluctuations, in which a SIT is driven by the breaking of Cooper pairs and the localization of electrons, forming a Fermi insulator [8–11]. On the other hand, the SIT in the bosonic description is driven by fluctuations of the phase, in which the superconducting and the insulating states with different symmetry are separated by a QCP [12–14]. On the superconducting side of such a transition, the Cooper pairs are mobile. Magnetic vortices are localized and can be bound into vortex-antivortex pairs [4]. On the insulating side, the vortices are mobile but the Cooper pairs are localized, forming a Bose insulating state [13–16]. A number of SIT experiments suggest that the localization of Cooper pairs leads to a quantum-percolation induced superconductor to Bose insulator transition, with a product of the correlation length and dynamical exponents $z\nu \sim 4/3$ near the quantum critical point [2,4,17–21]. However, a superconductor to Fermi insulator

transition has also been found in some experiments, with $z\nu \sim 2/3$ [5,6,22,23]. Although many SIT experiments driven by different control parameters have been reported for a variety of materials and with varying $z\nu$ products, the nature of the nonsuperconducting ground states at zero temperature and the reason for the difference in the respective $z\nu$ values are still unclear [2,24].

In this paper, we study the superconductor to insulator transition in an amorphous $\text{W}_{0.75}\text{Si}_{0.25}$ film with thickness $d \approx 5$ nm. While the details of its preparation are described in Ref. [25], we provide more information about the morphology of the film in Supplemental Material S1 [26]. Since d is smaller than the coherence length (≈ 7 nm), we can classify it as quasi-two-dimensional (quasi-2D) [28]. Further support for the quasi-2D behavior comes from fits of the fluctuation resistivity near the critical temperature $T_c \sim 3.95$ K (see Supplemental Material S2 [29]). We demonstrate that a perpendicular magnetic field drives the quasi-2D amorphous $\text{W}_{0.75}\text{Si}_{0.25}$ film into an insulating state in two stages, as it is shown in Fig. 1. At a critical field $B_c^1 = 6.25$ T, the sheet resistance R_s is independent of temperature in the zero-temperature limit, which is a hallmark of a QPT, and the superconducting state is driven into an insulating state. Above B_c^1 , namely, on the insulating side of the QPT, pronounced superconducting fluctuations still exist in the system, persisting up to $T \sim 5$ K, well above the zero-field critical temperature $T_c \sim 3.95$ K of the film, as it is shown in Figs. 1(a) and 1(b). With increasing the magnetic field further, the superconducting fluctuations gradually diminish, and a second classical transition occurs at a critical field $B_c^2 = 7.3$ T, above which the superconducting fluctuations disappear [see Fig. 1(c)]. We will interpret the classical critical field B_c^2 as a transition to a Fermi insulator.

An experimental characteristic for such transitions is the scaling behavior of physical quantities [1,2]. When the system

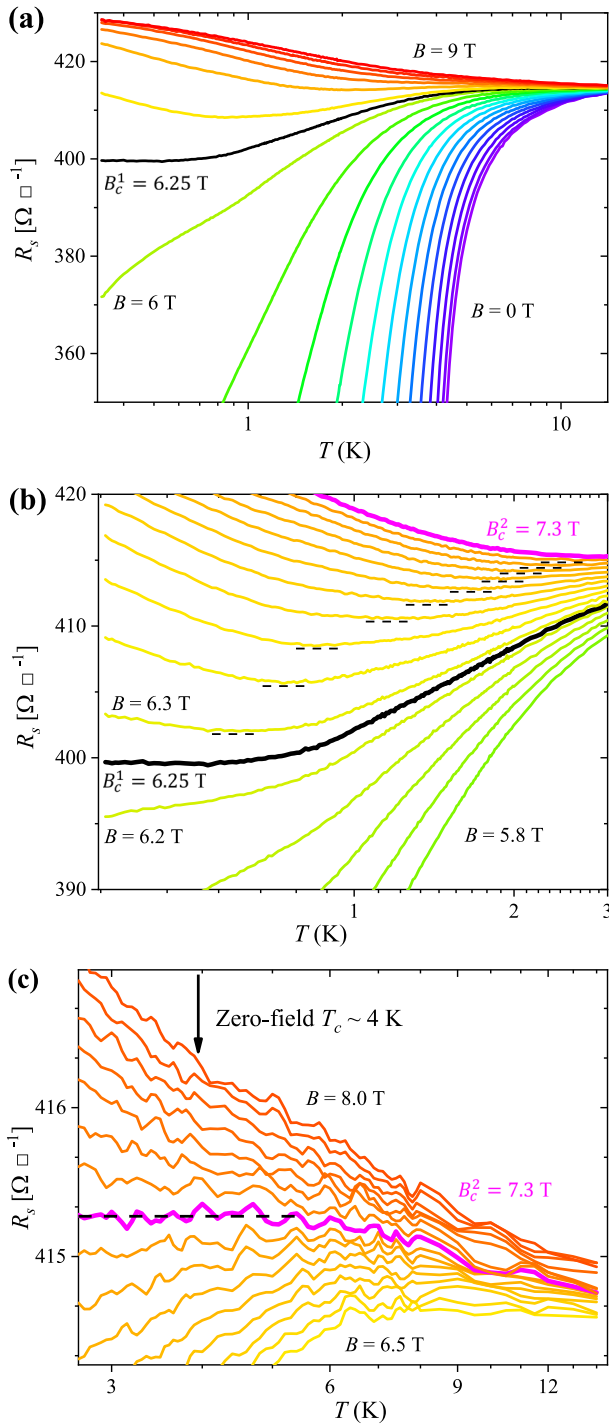


FIG. 1. Magnetic-field-driven superconductor to insulator transition. (a) Sheet resistance R_s as a function of temperature for different magnetic fields from 0 to 9 T in steps of 0.5 T. The $R_s(T)$ at the critical field B_c^1 is shown as a black line. (b) Detailed $R_s(T)$ data in steps of 0.1 T showing the characteristic magnetic field B_c^1 for which R_s is constant from $T \sim 0.6$ K down to the zero-temperature limit. The minima in the $R_s(T)$ data, which define the boundary between the Bose insulating state and the normal phase, are marked with dashed lines. (c) Corresponding $R_s(T)$ data for $B > B_c^1$, showing the characteristic magnetic field B_c^2 separating the Bose insulating state with pronounced superconducting fluctuations, from the Fermi insulating state. Above B_c^2 , there are no signs of superconducting fluctuations.

enters the critical region close to the phase transition, the measured physical quantities show a power-law dependence on the rescaled spatial and time coordinates, i.e., the correlation length ξ (depending on the proximity to the phase transition point, $\xi \sim |x - x_c|^{-\nu}$) and correlation time τ ($\tau \propto \xi^z \propto |x - x_c|^{-z\nu}$). These two scaling parameters ξ and τ , which both diverge at the transition point, are determined by the microscopic parameters in the Hamiltonian describing the system. The correlation length exponent ν and dynamical critical exponent z , as well as the scaling functions, however, are determined only by the universality class of phase transition, which depends only on the general properties of the system, such as the space dimensionality d , presence of disorder, and the symmetry of the order-parameter manifold [2–4]. For a magnetic-field-driven SIT, the sheet resistance can be rescaled as $R_s(B, T) \propto |B - B_c|^{2-d} F(|B - B_c|T^{-1/z\nu})$, with an arbitrary but for the system universal scaling function $F(x)$ with $F(0) = 1$. In the 2D ($d = 2$) limit, ξ drops out, R_s at the critical point becomes universal (R_Q), and $R_s(B, T) = R_Q F(|B - B_c|T^{-1/z\nu})$, where $R_Q = h/4e^2$ is the quantum resistance for Cooper pairs [3].

Figure 2(a) shows the magnetoresistance R_s data for temperatures ranging from 0.34 to 0.54 K. The $R_s(B)$ curves clearly exhibit a crossing point at a critical magnetic field ($B_c^1 = 6.25$ T, $R_c^1 = 399.7 \Omega$). It corresponds to the separatrix with a constant $R_s(T)$ in the zero-temperature limit, thereby defining the QCP in Fig. 1(b). This critical point separates the insulating state from the superconducting state, in that dR_s/dT changes its sign from superconducting behavior to insulating behavior at different sides of B_c^1 . In the critical regime, the $R_s(B, T)$ data should collapse onto a single curve by scaling the abscissa as $|B - B_c^1|t$, where $t = T^{-1/z\nu}$ [2,24]. Here we set t at the lowest investigated temperature as $t(0.34 \text{ K}) = 1$, and all the other data are then collapsed onto $R_s(B, T = 0.34 \text{ K})$ by adjusting t for each temperature T , as it is shown in Fig. 2(b). As a result, the critical exponent $z\nu$ can be retrieved by a power-law fit of $t(T)$, which yields $z\nu = 1.33 \sim 4/3$ with high precision on both sides of the SIT [Fig. 2(b), inset]. Alternatively, a critical exponent $z\nu \sim 4/3$ can also be obtained from scaling other parameters, such as $T_c(B)$. By carefully checking the $T_c(B)$ dependence in the zero-temperature limit, the QCP ($B_c^1, T = 0$) is very close to the extrapolated ending point of the $T_c(B)$ curve (see Fig. 4), which is consistent with theoretical expectations [17]. According to general scaling arguments [3,23], the thermodynamic superconducting transition temperature $T_c(B)$ scales in the vicinity of the QCP according to $T_c(B) \propto |B - B_c^1|^{z\nu}$, which we indeed observe with $z\nu \sim 4/3$ [see more details about the $T_c(B)$ scaling near B_c^1 in Supplemental Material S3 [30]].

Above the QCP B_c^1 , superconducting fluctuations still persist in the system at finite temperatures [Fig. 1(b)], but the system is a zero-temperature insulator. At finite temperatures, the $R_s(T)$ data [Figs. 1(b) and 1(c)] show a minimum, separating the fluctuations dominated region [$dR_s(T)/dT > 0$] from the insulating region [$dR_s(T)/dT < 0$], thereby defining a phase boundary between the Bose insulating and the fluctuation dominated normal state (see Fig. 4). Such finite temperature superconducting fluctuations beyond the superconductor to insulator QPTs have also been observed in amorphous InO_x systems [17], liquid helium-quenched gallium films [32], and

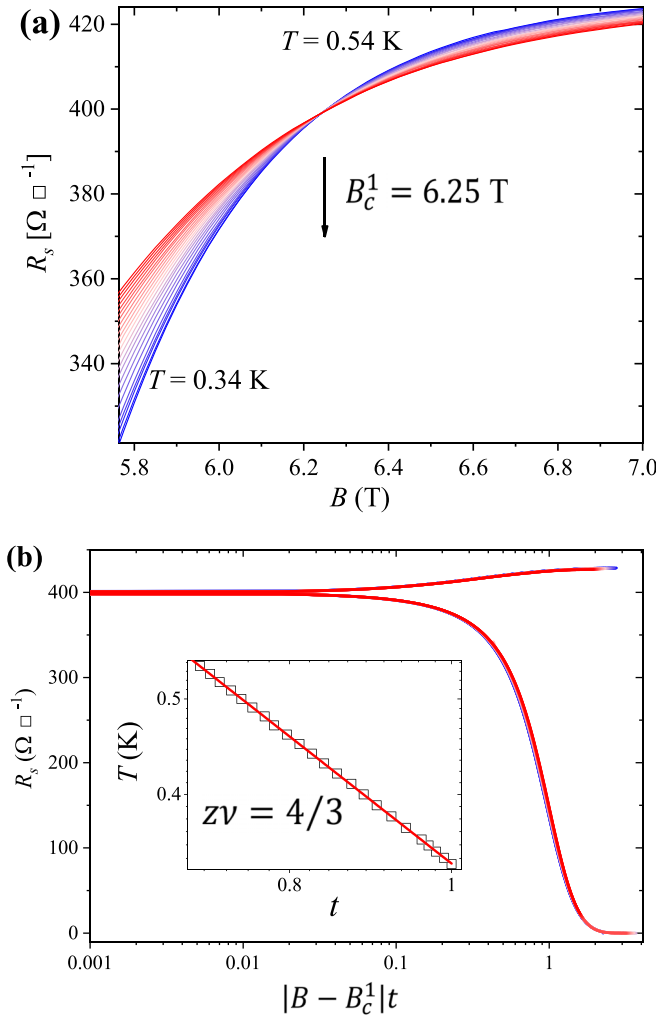


FIG. 2. Scaling analysis at B_c^1 . (a) Sheet resistance R_s as a function of magnetic field B for different temperatures from 0.34 to 0.54 K. The crossing point is at $B_c^1 = 6.25$ T, $R_c^1 = 399.7 \Omega/\square$. (b) Scaling-analysis plot of R_s as a function of $|B - B_c^1|t$. The scaling analysis is performed in fields ranging from 0 to 9 T, which is based on the best data collapse near the critical point. Inset: Temperature dependence of the scaling parameter t , with a power-law fit according to $z\nu = 4/3$ (solid line).

quench-condensed ultrathin beryllium films [20]. The superconducting fluctuations above B_c^1 are gradually weakened by increasing the magnetic field until a second critical field ($B_c^2 = 7.3$ T, $R_c^2 = 415.3 \Omega$) is reached, beyond which the superconducting fluctuations disappear [Fig. 1(c)]. Inspecting the corresponding $R_s(B, T)$ data in the temperature range from 3 to 5 K [Fig. 3(a)] reveals another crossing point at B_c^2 , which we interpret as the critical value for Cooper-pair breaking, i.e., the transition to a Fermi insulating state. The scaling analysis in the critical regime of B_c^2 , analogous to that applied at B_c^1 , shows an excellent collapse of the $R_s(B, T)$ curves [Fig. 3(b)], leading to $z\nu = 0.67 \sim 2/3$ [Fig. 3(b), inset].

It is natural to interpret our observations in the following way. The perfect scaling behavior down to zero temperature at B_c^1 is clearly consistent with the bosonic description, where Cooper pairs exist on both sides of the superconductor to insulator QPT which is driven by quantum phase

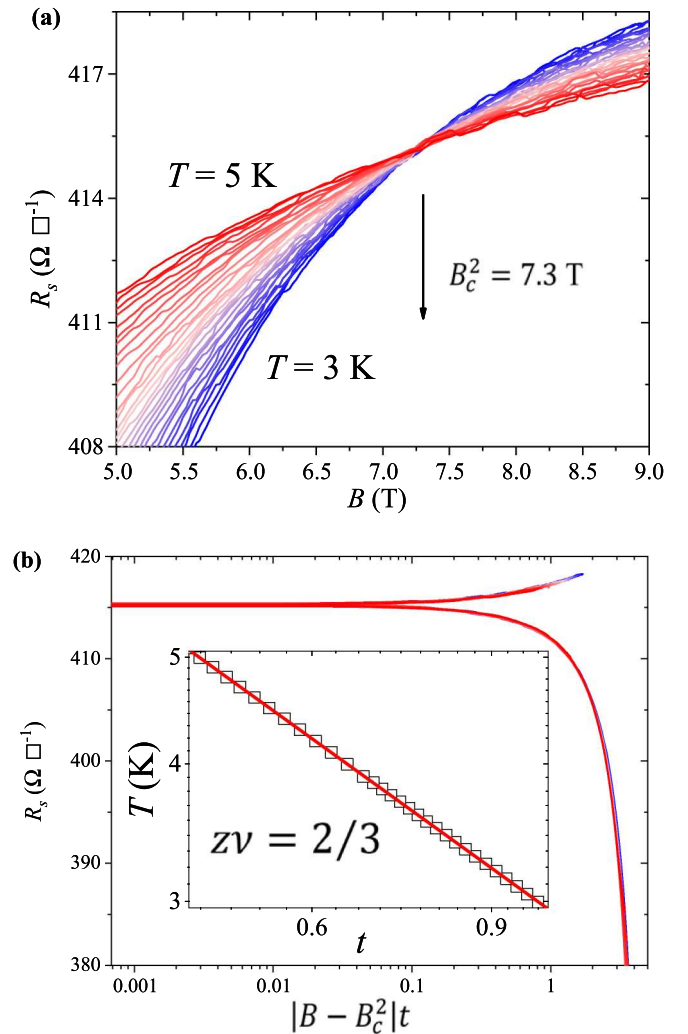


FIG. 3. Scaling analysis at B_c^2 . (a) Sheet resistance R_s as a function of magnetic field B for different temperatures between 3 and 5 K, with a distinct crossing point at ($B_c^2 = 7.3$ T, $R_c^2 = 415.3 \Omega/\square$). (b) Scaling-analysis plot of R_s as a function of $|B - B_c^2|t$ for fields from 4 to 9 T. Inset: Temperature dependence of the scaling parameter t , with $z\nu = 2/3$.

fluctuations [2–4,13,14,24]. The zero-temperature insulating state is characterized by the loss of global phase coherence. However, superconducting amplitude fluctuations still exist on the insulating side above B_c^1 [33,34]. The physical picture on the insulating side involves localized Cooper pairs and freely moving vortices, forming a bosonic insulating state [2,13,14]. The product $z\nu = 4/3$ is the simplest and most direct manifestation of such a superconductor to Bose insulator QPT since it only depends on the universality class of the system. By assuming $z = 1$, $\nu \sim 4/3 > 1$ corresponds to the $T \rightarrow 0$ SIT in 2D disordered systems, as observed in some conventional amorphous superconductors [18,35], two-dimensional electron gases at oxide interfaces [24], ultrathin high- T_c superconductors [4,21], or, more recently, in graphene-metal hybrids [36]. The critical sheet resistance $R_c \approx 400 \Omega$ measured in our amorphous WSi film at B_c^1 is one order of magnitude smaller than $R_Q \approx 6$ k Ω , however. We note that certain deviations of experimental R_c from the ideal theoretical value R_Q are

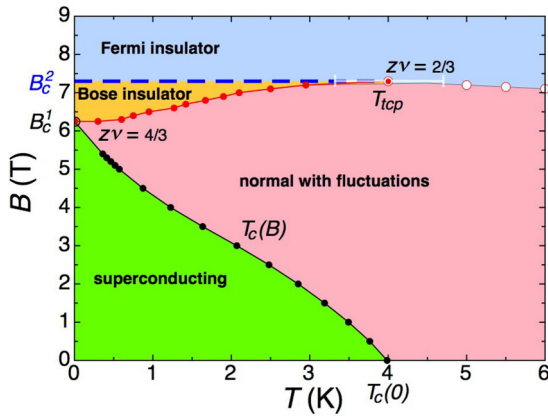


FIG. 4. Sketch of the superconductor to insulator transition in the B - T phase diagram. The boundary between the Bose insulating state and the fluctuation-dominated normal state (filled red circles) is determined by the minimum of the $R_s(T)$ curves at different fields between B_c^1 and B_c^2 . The separation between the Fermi insulating state and the fluctuation-dominated normal state (open circles) is defined by the maximum of the $R_s(T)$ curves beyond $T_c(0)$. The tricritical point at T_{TCP} is approximately located at $T_c(0)$, but with a large error margin.

not uncommon, and can be ascribed to the contribution of a Fermionic channel to the total resistance [18].

Above B_c^1 on the insulating side, the sizeable superconducting fluctuations must be attributed to localized Cooper pairs in superconducting islands. In disordered or even amorphous superconductors which can be rendered into an inhomogeneous state by order-parameter amplitude fluctuations, such superconducting islands can appear in the system in high magnetic fields [2,28,29,37]. At a critical field B_c^2 , the localized Cooper pairs are completely destroyed, and a $z\nu \sim 2/3$ classical transition to Fermi insulator occurs. Such transitions with $z\nu \sim 2/3$ and driven by a perpendicular magnetic field have also been observed in other conventional 2D films, such as a -NbSi [22], a -bismuth [38], or in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ films [21]. A comparison of our a -WSi with a -NbSi, a -bismuth, and $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ (H_1^* in Ref. [21]) reveals a very similar behavior with respect to the classical critical field B_c^2 , in which the critical regions are actually located near $T_c(0)$. Other SITs with $z\nu \sim 2/3$ have been found in electrostatically tuned superconducting $\text{LaTiO}_3/\text{SrTiO}_3$ or $\text{LaAlO}_3/\text{SrTiO}_3$ interfaces [23,24]. At the $\text{LaTiO}_3/\text{SrTiO}_3$ interfaces, the global superconductivity is

supposed to be determined by the presence of superconducting islands coupled by nonsuperconducting metallic regions, and the magnetic-field-driven SIT with $z\nu \sim 2/3$ corresponds to the vanishing of Cooper pairs within the islands [24]. At the electrical field stimulated $\text{LaAlO}_3/\text{SrTiO}_3$ superconducting interfaces, the charge-density-driven superconductor to Fermi insulator transition with $z\nu \sim 2/3$ at large negative electrical field can be ascribed to the depletion of carriers and breaking of Cooper pairs [23].

The scenarios in which SITs with $z\nu \sim 2/3$ correspond to a phase transition associated with pair breaking are further supported by the magnetic-field-tuned SITs with varying bias current in 2D beryllium films [20]. At negligible bias current, an SIT with $z\nu \sim 4/3$ is observed, while with a dc current near the zero-field depairing critical currents the $z\nu$ is driven from $\sim 4/3$ to $\sim 2/3$ [20].

The phase transitions among these distinct states in our WSi films are visualized in the schematic phase diagram in Fig. 4. At low field, the superconducting state and the fluctuation-dominated normal region are separated by the $T_c(B)$ line, which we experimentally determined by a $R_n/2$ standard. This $T_c(B)$ line terminates at the QCP B_c^1 in the zero-temperature limit as $T_c(B) \propto |B - B_c^1|^{z\nu}$. At zero temperature, the superconducting and the Bose insulating quantum ground state are separated by the QPT at B_c^1 . Above B_c^1 and at elevated temperatures, finite temperature classical transitions between the fluctuation-dominated normal and the Bose insulating states are observed. They end at the second critical field B_c^2 and at a tricritical point around $T_{TCP} \approx T_c(0) \approx 4$ K. At temperatures above T_{TCP} , the fluctuation-dominated state directly crosses over into the Fermi insulating state. At low temperatures, the localized Cooper pairs within the superconducting islands in the Bose insulating state are subsequently destroyed by the increasing field, and a Bose insulator to Fermi insulator transition occurs. By carefully comparing the response of the $R_s(B)$ data to the magnetic field near B_c^1 and B_c^2 , we state that the crossover between Bose insulating (strong field dependence) and Fermi insulating state (weak field dependence) must correspond to a virtually horizontal line terminating at the tricritical point at T_{TCP} (Fig. 4; see more details about the crossover in Supplemental Material S4 [39]), which characterizes the field B_c^2 as the depairing field of the Cooper pairs.

This paper was supported by UZH and Swiss National Foundation Project No. 20-175554. We acknowledge A. Goldman, T. Neupert, J. Chang, Q. Wang, and D. Destraz for discussions. We thank H. Ma for assistance in sample characterization.

- [1] S. L. Sondhi, S. M. Girvin, J. P. Carini, and D. Shahar, Continuous quantum phase transitions, *Rev. Mod. Phys.* **69**, 315 (1997).
- [2] A. M. Goldman, Superconductor-insulator transitions, *Int. J. Mod. Phys. B* **24**, 4081 (2010).
- [3] V. F. Gantmakher and V. T. Dolgoplov, Superconductor-insulator quantum phase transition, *Phys.-Usp.* **53**, 1 (2010).
- [4] A. T. Bollinger, G. Dubuis, J. Yoon, D. Pavuna, J. Misewich, and I. Bozović, Superconductor-insulator transition in

$\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ at the pair quantum resistance, *Nature (London)* **472**, 458 (2011).

- [5] N. Marković, C. Christiansen, and A. M. Goldman, Thickness-Magnetic Field Phase Diagram at the Superconductor-Insulator Transition in 2D, *Phys. Rev. Lett.* **81**, 5217 (1998).
- [6] K. A. Parendo, K. H. Sarwa B. Tan, A. Bhattacharya, M. EblenZayas, N. E. Staley, and A. M. Goldman, Electrostatic Tuning of the Superconductor-Insulator Transition in Two Dimensions, *Phys. Rev. Lett.* **94**, 197004 (2005).

- [7] B. Sacépé, T. Dubouchet, C. Chapelier, M. Sanquer, M. Ovdia, D. Shahar, M. Feigelman, and L. Ioffe, Localization of preformed Cooper pairs in disordered superconductors, *Nat. Phys.* **7**, 239 (2011).
- [8] J. M. Valles, Jr., R. C. Dynes, and J. P. Garno, Electron Tunneling Determination of the Order-Parameter Amplitude at the Superconductor-Insulator Transition in 2D, *Phys. Rev. Lett.* **69**, 3567 (1992).
- [9] A. M. Finkel'stein, Suppression of superconductivity in homogeneously disordered systems, *Physica B* **197**, 636 (1994).
- [10] S. Y. Hsu, J. A. Chervenak, and J. M. Valles, Jr., Magnetic Field Enhanced Order Parameter Amplitude Fluctuations in Ultrathin Films Near the Superconductor-Insulator Transition, *Phys. Rev. Lett.* **75**, 132 (1995).
- [11] P. Szabó, T. Samuely, V. Hašková, J. Kačmarčík, M. Žemlička, M. Grajcar, J. G. Rodrigo, and P. Samuely, Fermionic scenario for the destruction of superconductivity in ultrathin MoC films evidenced by STM measurements, *Phys. Rev. B* **93**, 014505 (2016).
- [12] D. B. Haviland, Y. Liu, and A. M. Goldman, Onset of Superconductivity in the Two-Dimensional Limit, *Phys. Rev. Lett.* **62**, 2180 (1989).
- [13] M. P. A. Fisher, G. Grinstein, and S. M. Girvin, Presence of Quantum Diffusion in Two Dimensions: Universal Resistance at the Superconductor-Insulator Transition, *Phys. Rev. Lett.* **64**, 587 (1990).
- [14] M. P. A. Fisher, Quantum Phase Transitions in Disordered Two-Dimensional Superconductors, *Phys. Rev. Lett.* **65**, 923 (1990).
- [15] M. Ovdia, D. Kalok, B. Sacépé, and D. Shahar, Duality symmetry and its breakdown in the vicinity of the superconductor-insulator transition, *Nat. Phys.* **9**, 415 (2013).
- [16] X. G. Wen and A. Zee, Universal conductance at the superconductor-insulator transition, *Int. J. Mod. Phys. B* **4**, 437 (1990).
- [17] A. F. Hebard and M. A. Paalanen, Magnetic-Field-Tuned Superconductor-Insulator Transition in Two-Dimensional Films, *Phys. Rev. Lett.* **65**, 927 (1990).
- [18] A. Yazdani and A. Kapitulnik, Superconducting-Insulating Transition in Two Dimensional a -Mogé Thin Films, *Phys. Rev. Lett.* **74**, 3037 (1995).
- [19] N. Mason and A. Kapitulnik, Dissipation Effects on the Superconductor-Insulator Transition in 2D Superconductors, *Phys. Rev. Lett.* **82**, 5341 (1999).
- [20] E. Bielejec and W. Wu, Field-Tuned Superconductor-Insulator Transition with and without Current Bias, *Phys. Rev. Lett.* **88**, 206802 (2002).
- [21] X. Shi, P. V. Lin, T. Sasagawa, V. Dobrosavljević, and D. Popović, Two-stage magnetic-field-tuned superconductor-insulator transition in underdoped $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$, *Nat. Phys.* **10**, 437 (2014).
- [22] H. Aubin, C. A. Marrache-Kikuchi, A. Pourret, K. Behnia, L. Bergé, L. Dumoulin, and J. Lesueur, Magnetic-field-induced quantum superconductor-insulator transition in $\text{Nb}_{0.15}\text{Si}_{0.85}$, *Phys. Rev. B* **73**, 094521 (2006).
- [23] A. D. Caviglia, S. Gariglio, N. Reyren, D. Jaccard, T. Schneider, M. Gabay, S. Thiel, G. Hammerl, J. Mannhart, and J.-M. Triscone, Electric field control of the $\text{LaAlO}_3/\text{SrTiO}_3$ interface ground state, *Nature (London)* **456**, 624 (2008).
- [24] J. Biscaras, N. Bergeal, S. Hurand, C. Feuillet-Palma, A. Rastogi, R. C. Budhani, M. Grilli, S. Caprara, and J. Lesueur, Multiple quantum criticality in a two-dimensional superconductor, *Nat. Mater.* **12**, 542 (2013).
- [25] X. Zhang, A. Engel, Q. Wang, A. Schilling, A. Semenov, M. Sidorova, H.-W. Hübers, I. Charaev, K. Ilin, and M. Siegel, Characteristics of superconducting tungsten silicide $\text{W}_x\text{Si}_{1-x}$ for single photon detection, *Phys. Rev. B* **94**, 174509 (2016).
- [26] See Supplemental Material S1 at <http://link.aps.org/supplemental/10.1103/PhysRevB.97.214524> for the detailed description of the amorphous morphology of the WSi film. Also see Ref. [27].
- [27] F. Marsili, V. B. Verma, J. A. Stern, S. Harrington, A. E. Lita, T. Gerrits, I. Vayshenker, B. Baek, M. D. Shaw, R. P. Mirin, and S. W. Nam, Detecting single infrared photons with 93% system efficiency, *Nat. Photonics* **7**, 210 (2013).
- [28] M. Tinkham, *Introduction to Superconductivity* (McGraw-Hill, New York, 1975).
- [29] See Supplemental Material S2 at <http://link.aps.org/supplemental/10.1103/PhysRevB.97.214524> for the detailed comparison of the 2D and 3D fits to the fluctuation sheet resistance just above T_c of the 5-nm-thick WSi film.
- [30] See Supplemental Material S3 at <http://link.aps.org/supplemental/10.1103/PhysRevB.97.214524> for the detailed description of the $T_c(B)$ scaling near B_c^1 . Also see Ref. [31].
- [31] Y. Xing, H.-M. Zhang, H.-L. Fu, H. Liu, Y. Sun, J.-P. Peng, F. Wang, X. Lin, X.-C. Ma, Q.-K. Xue, J. Wang, and X. C. Xie, Quantum Griffiths singularity of superconductor-metal transition in Ga thin films, *Science* **350**, 542 (2015).
- [32] C. Christiansen, L. M. Hernandez, and A. M. Goldman, Evidence of Collective Charge Behavior in the Insulating State of Ultrathin Films of Superconducting Metals, *Phys. Rev. Lett.* **88**, 037004 (2002).
- [33] P. Phillips and D. Dalidovich, The elusive Bose metal, *Science* **302**, 243 (2003).
- [34] P. Phillips, Two-dimensional materials: Not just a phase, *Nat. Phys.* **12**, 206 (2016).
- [35] M. A. Steiner, N. P. Breznay, and A. Kapitulnik, Approach to a superconductor-to-Bose-insulator transition in disordered films, *Phys. Rev. B* **77**, 212501 (2008).
- [36] A. Allain, Z. Han, and V. Bouchiat, Electrical control of the superconducting-to-insulating transition in graphene-metal hybrids, *Nat. Mater.* **11**, 590 (2012).
- [37] Y. Dubi, Y. Meir, and Y. Avishai, Nature of the superconductor-insulator transition in disordered superconductors, *Nature (London)* **449**, 876 (2007).
- [38] N. Marković, C. Christiansen, A. M. Mack, W. H. Huber, and A. M. Goldman, Superconductor-insulator transition in two dimensions, *Phys. Rev. B* **60**, 4320 (1999).
- [39] See Supplemental Material S4 at <http://link.aps.org/supplemental/10.1103/PhysRevB.97.214524> for the detailed description of the crossover between the Bose insulating state and the Fermi insulating state. Also see Ref. [40].
- [40] G. Bergmann, Physical interpretation of weak localization: A time-of-flight experiment with conduction electrons, *Phys. Rev. B* **28**, 2914 (1983).